

right triangle trig review answer key

Right Triangle Trig Review Answer Key

Right triangle trigonometry is a foundational concept in mathematics that is widely used in various fields, including physics, engineering, architecture, and computer graphics. Understanding the relationships between the angles and sides of right triangles allows students and professionals alike to solve complex problems. This article serves as a comprehensive review of right triangle trigonometry, providing an answer key to common problems, essential formulas, and explanations that will help reinforce your understanding of the subject.

Understanding Right Triangles

A right triangle is defined as a triangle that has one angle measuring 90 degrees. The sides of a right triangle are categorized as follows:

- Hypotenuse: The side opposite the right angle, which is the longest side of the triangle.
- Adjacent Side: The side that is next to the angle of interest that is not the hypotenuse.
- Opposite Side: The side that is opposite to the angle of interest.

The relationship between these sides can be explored through trigonometric functions: sine (sin), cosine (cos), and tangent (tan).

Key Trigonometric Ratios

The three primary trigonometric functions associated with right triangles are defined as follows:

1. Sine (sin):
- Formula: $\sin(\theta) = \frac{\text{Opposite}}{\text{Hypotenuse}}$
2. Cosine (cos):
- Formula: $\cos(\theta) = \frac{\text{Adjacent}}{\text{Hypotenuse}}$
3. Tangent (tan):
- Formula: $\tan(\theta) = \frac{\text{Opposite}}{\text{Adjacent}}$

These ratios serve as the basis for solving right triangle problems, allowing for the calculation of unknown side lengths or angles when certain values are known.

Common Right Triangle Problems

To solidify your understanding of right triangle trigonometry, let's explore some common problems and their solutions.

Problem 1: Finding the Hypotenuse

Given a right triangle with an angle θ of 30 degrees and an opposite side of length 5 units, find the length of the hypotenuse.

Solution:

Using the sine function:

$$\sin(30^\circ) = \frac{5}{\text{Hypotenuse}}$$

We know that $\sin(30^\circ) = 0.5$:

$$0.5 = \frac{5}{\text{Hypotenuse}}$$

Multiplying both sides by the hypotenuse:

$$0.5 \cdot \text{Hypotenuse} = 5$$

Dividing by 0.5 gives us:

$$\text{Hypotenuse} = 10 \text{ units}$$

Problem 2: Finding the Opposite Side

Given a right triangle with an angle θ of 45 degrees and a hypotenuse of length 14 units, find the length of the opposite side.

Solution:

Using the sine function:

$$\sin(45^\circ) = \frac{\text{Opposite}}{14}$$

We know that $\sin(45^\circ) = \frac{\sqrt{2}}{2}$:

$$\frac{\sqrt{2}}{2} = \frac{\text{Opposite}}{14}$$

Multiplying both sides by 14 gives us:

$$\begin{aligned} \text{Opposite} &= 14 \cdot \frac{\sqrt{2}}{2} = 7\sqrt{2} \text{ units} \\ &\approx 9.9 \text{ units} \end{aligned}$$

Problem 3: Finding the Adjacent Side

Given a right triangle with an angle θ of 60 degrees and an opposite side of length 8 units, find the length of the adjacent side.

Solution:

Using the tangent function:

$$\tan(60^\circ) = \frac{8}{\text{Adjacent}}$$

We know that $\tan(60^\circ) = \sqrt{3}$:

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\[
\sqrt{3} = \frac{8}{\text{Adjacent}}
\]
Multiplying both sides by the adjacent side:
\[
\sqrt{3} \cdot \text{Adjacent} = 8
\]
Dividing by  $(\sqrt{3})$  gives us:
\[
\text{Adjacent} = \frac{8}{\sqrt{3}} \approx 4.62 \text{ units}
\]

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Special Right Triangles

There are two special types of right triangles that are particularly important in trigonometry:

1. 30-60-90 Triangle

In a 30-60-90 triangle, the sides are in a specific ratio:

- The side opposite the 30-degree angle is (x) .
- The side opposite the 60-degree angle is $(x\sqrt{3})$.
- The hypotenuse is $(2x)$.

For example, if the side opposite the 30-degree angle is 5 units, the lengths of the other sides would be:

- Opposite 60 degrees: $(5\sqrt{3} \approx 8.66)$ units.
- Hypotenuse: (10) units.

2. 45-45-90 Triangle

In a 45-45-90 triangle, the sides are also in a specific ratio:

- Both legs are equal in length and can be represented as (x) .
- The hypotenuse is $(x\sqrt{2})$.

For example, if each leg is 7 units, the hypotenuse would be:

- Hypotenuse: $(7\sqrt{2} \approx 9.9)$ units.

Practice Problems and Answer Key

To further your understanding of right triangle trigonometry, here are some practice problems along with their answers.

Problem Set

1. Given a right triangle with an angle of 40 degrees and an adjacent side of 10 units, find the length of the opposite side.

2. Find the hypotenuse of a triangle with an angle of 70 degrees and an opposite side of 9 units.
3. In a 45-45-90 triangle, if one leg measures 6 units, what is the length of the hypotenuse?

Answer Key

1. Using the tangent function:

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\[
\tan(40^\circ) = \frac{\text{Opposite}}{10} \implies \text{Opposite} = 10
\tan(40^\circ) \approx 8.43 \text{ units}
\]
```

2. Using the sine function:

```
\[
\sin(70^\circ) = \frac{9}{\text{Hypotenuse}} \implies \text{Hypotenuse} =
\frac{9}{\sin(70^\circ)} \approx 9.46 \text{ units}
\]
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3. For a 45-45-90 triangle:

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\[
\text{Hypotenuse} = 6\sqrt{2} \approx 8.49 \text{ units}
\]
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Conclusion

Right triangle trigonometry is an essential and versatile area of mathematics that provides tools for solving real-world problems. By understanding the relationships between the angles and sides of right triangles, and utilizing trigonometric functions, students can approach a variety of challenges with confidence. Through practice problems, special triangles, and the application of trigonometric ratios, mastery of right triangle trigonometry is within reach. Remember, practice is key to success, so continue to work through problems to solidify your understanding and enhance your skills.

Frequently Asked Questions

What is the Pythagorean theorem and how is it used in right triangle trigonometry?

The Pythagorean theorem states that in a right triangle, the square of the length of the hypotenuse is equal to the sum of the squares of the lengths of the other two sides ($a^2 + b^2 = c^2$). It's used to find the length of one side when the lengths of the other two sides are known.

What are the primary trigonometric ratios used in right triangles?

The primary trigonometric ratios are sine (sin), cosine (cos), and tangent

(tan). They are defined as follows: $\sin(\theta) = \text{opposite/hypotenuse}$, $\cos(\theta) = \text{adjacent/hypotenuse}$, and $\tan(\theta) = \text{opposite/adjacent}$.

How can you find the angle measures in a right triangle using trigonometric ratios?

You can find the angle measures by using the inverse trigonometric functions: arcsin, arccos, and arctan. For example, to find angle θ , you can use $\theta = \arcsin(\text{opposite/hypotenuse})$, $\theta = \arccos(\text{adjacent/hypotenuse})$, or $\theta = \arctan(\text{opposite/adjacent})$.

What is the relationship between the special right triangles (30-60-90 and 45-45-90)?

In a 30-60-90 triangle, the side lengths are in the ratio $1:\sqrt{3}:2$, while in a 45-45-90 triangle, the side lengths are in the ratio $1:1:\sqrt{2}$. These ratios can be used to quickly find side lengths based on one known side.

What is the significance of SOH-CAH-TOA in right triangle trigonometry?

SOH-CAH-TOA is a mnemonic that helps remember the definitions of the sine, cosine, and tangent functions: SOH (Sine = Opposite/Hypotenuse), CAH (Cosine = Adjacent/Hypotenuse), and TOA (Tangent = Opposite/Adjacent).

How do you apply the Law of Cosines and Law of Sines in right triangles?

In right triangles, the Law of Cosines simplifies to the Pythagorean theorem ($c^2 = a^2 + b^2$). The Law of Sines can be used to find unknown angles or sides when you have a non-right triangle, but it's not typically necessary for right triangles since trigonometric ratios are more straightforward.

What are some common applications of right triangle trigonometry in real life?

Right triangle trigonometry has applications in various fields including architecture, engineering, navigation, and physics. It is used to calculate heights, distances, angles, and in constructing models.

How do you utilize the unit circle to understand right triangle trigonometry?

The unit circle helps visualize the sine and cosine values for different angles. Each point on the unit circle corresponds to a right triangle with a hypotenuse of 1, allowing easy determination of the sine (y-coordinate) and cosine (x-coordinate) for any angle.

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