

# MODULAR FUNCTIONS AND DIRICHLET SERIES IN NUMBER THEORY

**MODULAR FUNCTIONS AND DIRICHLET SERIES IN NUMBER THEORY** FORM FUNDAMENTAL CONCEPTS THAT HAVE DEEPLY INFLUENCED MODERN MATHEMATICAL RESEARCH, ESPECIALLY IN THE REALM OF ANALYTIC NUMBER THEORY AND ARITHMETIC GEOMETRY. THESE TWO AREAS, WHILE DISTINCT, INTERTWINE THROUGH THEIR ROLE IN UNDERSTANDING THE PROPERTIES OF NUMBERS, PARTICULARLY PRIMES, AND THE STRUCTURES UNDERLYING MODULAR FORMS, L-FUNCTIONS, AND AUTOMORPHIC FORMS. MODULAR FUNCTIONS PROVIDE A RICH FRAMEWORK TO STUDY COMPLEX ANALYSIS ON MODULAR CURVES, WHEREAS DIRICHLET SERIES SERVE AS ESSENTIAL ANALYTIC TOOLS THAT ENCODE ARITHMETIC INFORMATION VIA INFINITE SERIES. THEIR INTERPLAY IS CRUCIAL IN ADVANCING TOPICS SUCH AS THE DISTRIBUTION OF PRIME NUMBERS, MODULARITY THEOREMS, AND THE EXPLICIT CONSTRUCTION OF L-FUNCTIONS. THIS ARTICLE EXPLORES THE DEFINITIONS, PROPERTIES, AND SIGNIFICANT APPLICATIONS OF MODULAR FUNCTIONS AND DIRICHLET SERIES IN NUMBER THEORY, SHEDDING LIGHT ON THEIR HISTORICAL DEVELOPMENT AND THEIR MODERN IMPLICATIONS. THE FOLLOWING SECTIONS DETAIL THE FOUNDATIONAL ASPECTS, ANALYTIC STRUCTURES, AND INTRICATE CONNECTIONS THAT MAKE THESE CONCEPTS INDISPENSABLE IN CONTEMPORARY MATHEMATICAL RESEARCH.

- FUNDAMENTALS OF MODULAR FUNCTIONS
- INTRODUCTION TO DIRICHLET SERIES
- CONNECTIONS BETWEEN MODULAR FUNCTIONS AND DIRICHLET SERIES
- APPLICATIONS IN NUMBER THEORY
- ADVANCED TOPICS AND RECENT DEVELOPMENTS

## FUNDAMENTALS OF MODULAR FUNCTIONS

MODULAR FUNCTIONS ARE COMPLEX FUNCTIONS DEFINED ON THE UPPER HALF-PLANE THAT EXHIBIT SPECIFIC TRANSFORMATION PROPERTIES UNDER THE ACTION OF MODULAR GROUPS, TYPICALLY  $SL(2, \mathbb{Z})$  OR ITS SUBGROUPS. THESE FUNCTIONS ARE INVARIANT OR TRANSFORM IN A CONTROLLED MANNER UNDER FRACTIONAL LINEAR TRANSFORMATIONS, MAKING THEM CENTRAL OBJECTS IN THE THEORY OF MODULAR FORMS. UNLIKE MODULAR FORMS, MODULAR FUNCTIONS MAY HAVE POLES BUT ARE MEROMORPHIC ON THE MODULAR CURVE. THEIR STUDY IS CLOSELY LINKED TO ELLIPTIC CURVES, COMPLEX TORI, AND THE THEORY OF RIEMANN SURFACES.

### DEFINITION AND BASIC PROPERTIES

A MODULAR FUNCTION IS A MEROMORPHIC FUNCTION  $f$  ON THE UPPER HALF-PLANE  $\mathbb{H}$  SATISFYING THE RELATION:

$$f\left(\frac{aT+b}{cT+d}\right) = f(T) \text{ FOR ALL MATRICES } \begin{bmatrix} a & b \\ c & d \end{bmatrix} \text{ IN A MODULAR GROUP, WHERE } T \in \mathbb{H}.$$

THESE FUNCTIONS ARE OFTEN STUDIED ON THE QUOTIENT SPACE FORMED BY THE ACTION OF THE MODULAR GROUP, RESULTING IN A MODULAR CURVE. THEY POSSESS A  $q$ -EXPANSION AT THE CUSP INFINITY, WHICH IS A FOURIER SERIES IN  $q = e^{2\pi i T}$ . THIS EXPANSION ENCODES SIGNIFICANT ARITHMETIC INFORMATION.

### EXAMPLES OF MODULAR FUNCTIONS

IMPORTANT EXAMPLES INCLUDE THE  $j$ -INVARIANT, WHICH CLASSIFIES ELLIPTIC CURVES OVER THE COMPLEX NUMBERS UP TO ISOMORPHISM. THE  $j$ -FUNCTION IS A MODULAR FUNCTION FOR THE FULL MODULAR GROUP  $SL(2, \mathbb{Z})$  AND PLAYS A PIVOTAL ROLE IN NUMBER THEORY AND ALGEBRAIC GEOMETRY.

- J-INVARIANT:** A FUNDAMENTAL MODULAR FUNCTION WITH A  $q$ -EXPANSION BEGINNING AS  $j(T) = q^{-1} + 744 +$

$$196884q + \dots$$

- **HAUPTMODULN:** MODULAR FUNCTIONS GENERATING THE FUNCTION FIELD OF MODULAR CURVES
- **MODULAR UNITS:** MODULAR FUNCTIONS WITH MULTIPLICATIVE INVERSES ALSO MODULAR FUNCTIONS

## INTRODUCTION TO DIRICHLET SERIES

DIRICHLET SERIES ARE INFINITE SERIES OF THE FORM  $\sum_{n=1}^{\infty} \frac{a_n}{n^s}$  WHERE  $s$  IS A COMPLEX VARIABLE AND  $a_n$  ARE COMPLEX COEFFICIENTS. THESE SERIES ARE VITAL IN ANALYTIC NUMBER THEORY BECAUSE THEY ENCODE ARITHMETIC FUNCTIONS AND FACILITATE THE STUDY OF THEIR DISTRIBUTION AND PROPERTIES THROUGH COMPLEX ANALYSIS TECHNIQUES. THE MOST FAMOUS EXAMPLE IS THE RIEMANN ZETA FUNCTION, WHICH PLAYS A CENTRAL ROLE IN THE DISTRIBUTION OF PRIME NUMBERS.

## DEFINITION AND CONVERGENCE

A DIRICHLET SERIES IS DEFINED AS:

$$D(s) = \sum_{n=1}^{\infty} \frac{a_n}{n^s} \text{ WHERE } s = \sigma + it \text{ IS A COMPLEX VARIABLE.}$$

THE REGION OF CONVERGENCE DEPENDS ON THE GROWTH OF THE COEFFICIENTS  $a_n$ . TYPICALLY, SUCH A SERIES CONVERGES ABSOLUTELY IN SOME HALF-PLANE  $\sigma > \sigma_0$ . ANALYTIC CONTINUATION AND FUNCTIONAL EQUATIONS OFTEN EXTEND THE DOMAIN WHERE THESE SERIES PROVIDE MEANINGFUL INFORMATION.

## KEY EXAMPLES

SEVERAL IMPORTANT ANALYTIC OBJECTS IN NUMBER THEORY ARE EXPRESSED AS DIRICHLET SERIES, INCLUDING:

- **RIEMANN ZETA FUNCTION:**  $\zeta(s) = \sum_{n=1}^{\infty} \frac{1}{n^s}$
- **DIRICHLET L-FUNCTIONS:**  $L(s, \chi) = \sum_{n=1}^{\infty} \frac{\chi(n)}{n^s}$  FOR DIRICHLET CHARACTERS  $\chi$
- **HECKE L-FUNCTIONS:** GENERALIZATIONS ASSOCIATED WITH MODULAR FORMS AND NUMBER FIELDS

## CONNECTIONS BETWEEN MODULAR FUNCTIONS AND DIRICHLET SERIES

THE PROFOUND RELATIONSHIP BETWEEN MODULAR FUNCTIONS AND DIRICHLET SERIES MANIFESTS PRIMARILY THROUGH MODULAR FORMS, WHICH ARE CLOSELY RELATED TO MODULAR FUNCTIONS BUT WITH HOLOMORPHICITY AND GROWTH CONDITIONS. MODULAR FORMS GIVE RISE TO L-FUNCTIONS REPRESENTED BY DIRICHLET SERIES WITH REMARKABLE ANALYTIC PROPERTIES. THESE L-FUNCTIONS ENCODE DEEP ARITHMETIC INFORMATION AND SATISFY FUNCTIONAL EQUATIONS AND ANALYTIC CONTINUATIONS THAT MIRROR THE MODULAR FORMS' SYMMETRIES.

## MODULAR FORMS AND ASSOCIATED L-FUNCTIONS

MODULAR FORMS ARE COMPLEX ANALYTIC FUNCTIONS ON THE UPPER HALF-PLANE WITH SPECIFIC TRANSFORMATION PROPERTIES AND GROWTH CONDITIONS. EACH MODULAR FORM CAN BE ASSOCIATED WITH A DIRICHLET SERIES CALLED AN L-FUNCTION, TYPICALLY CONSTRUCTED FROM ITS FOURIER COEFFICIENTS. THESE L-FUNCTIONS GENERALIZE THE RIEMANN ZETA FUNCTION AND DIRICHLET L-FUNCTIONS AND ARE CENTRAL IN MODERN NUMBER THEORY.

## ROLE OF THE MELLIN TRANSFORM

THE MELLIN TRANSFORM PROVIDES A BRIDGE BETWEEN MODULAR FORMS AND DIRICHLET SERIES. APPLYING THE MELLIN TRANSFORM TO THE FOURIER EXPANSION OF A MODULAR FORM YIELDS A DIRICHLET SERIES REPRESENTATION OF THE ASSOCIATED L-FUNCTION. THIS TRANSFORM IS CRUCIAL IN STUDYING ANALYTIC PROPERTIES SUCH AS CONTINUATION AND FUNCTIONAL EQUATIONS.

- TRANSFORMS FOURIER EXPANSIONS INTO DIRICHLET SERIES
- FACILITATES ANALYTIC CONTINUATION BEYOND THE REGION OF ABSOLUTE CONVERGENCE
- ENCODES MODULAR SYMMETRIES INTO FUNCTIONAL EQUATIONS OF L-FUNCTIONS

## APPLICATIONS IN NUMBER THEORY

THE INTERPLAY OF MODULAR FUNCTIONS AND DIRICHLET SERIES HAS LED TO SIGNIFICANT BREAKTHROUGHS AND APPLICATIONS IN NUMBER THEORY. THESE APPLICATIONS RANGE FROM PRIME NUMBER THEORY TO THE PROOF OF DEEP CONJECTURES INVOLVING ELLIPTIC CURVES AND MODULARITY.

## DISTRIBUTION OF PRIME NUMBERS

DIRICHLET L-FUNCTIONS, ARISING FROM CHARACTERS MODULO AN INTEGER, ARE INSTRUMENTAL IN GENERALIZING THE PRIME NUMBER THEOREM TO ARITHMETIC PROGRESSIONS. THE NON-VANISHING OF THESE L-FUNCTIONS ON CERTAIN LINES IN THE COMPLEX PLANE UNDERPINS THE DISTRIBUTION RESULTS FOR PRIMES IN SPECIFIC CONGRUENCE CLASSES.

## THE MODULARITY THEOREM

THE MODULARITY THEOREM, FORMERLY KNOWN AS THE TANIYAMA-SHIMURA-WEIL CONJECTURE, CONNECTS ELLIPTIC CURVES DEFINED OVER THE RATIONALS WITH MODULAR FORMS. IT ASSERTS THAT EVERY ELLIPTIC CURVE OVER  $\mathbb{Q}$  IS MODULAR, MEANING ITS L-FUNCTION COINCIDES WITH THE L-FUNCTION OF A MODULAR FORM. THIS THEOREM'S PROOF WAS A CORNERSTONE IN THE PROOF OF FERMAT'S LAST THEOREM AND HIGHLIGHTS THE ESSENTIAL CONNECTION BETWEEN MODULAR FUNCTIONS AND DIRICHLET SERIES REPRESENTING L-FUNCTIONS.

- CLASSIFICATION OF ELLIPTIC CURVES VIA MODULAR FORMS
- CONSTRUCTION OF L-FUNCTIONS FROM MODULAR PARAMETERIZATIONS
- IMPLICATIONS FOR RATIONAL POINTS AND ARITHMETIC GEOMETRY

## ADVANCED TOPICS AND RECENT DEVELOPMENTS

RESEARCH CONTINUES TO ADVANCE THE UNDERSTANDING OF MODULAR FUNCTIONS AND DIRICHLET SERIES IN NUMBER THEORY, WITH NEW GENERALIZATIONS AND APPLICATIONS EMERGING IN THE STUDY OF AUTOMORPHIC FORMS, MULTIPLE DIRICHLET SERIES, AND BEYOND.

# AUTOMORPHIC FORMS AND GENERALIZED L-FUNCTIONS

AUTOMORPHIC FORMS EXTEND THE CONCEPT OF MODULAR FORMS TO MORE GENERAL GROUPS AND HIGHER DIMENSIONS. THEIR ASSOCIATED L-FUNCTIONS, EXPRESSED AS DIRICHLET SERIES, GENERALIZE CLASSICAL CONSTRUCTIONS AND ARE AT THE FOREFRONT OF THE LANGLANDS PROGRAM, WHICH SEEKS TO UNIFY VARIOUS AREAS OF MATHEMATICS THROUGH DEEP CORRESPONDENCES.

## MULTIPLE DIRICHLET SERIES

MULTIPLE DIRICHLET SERIES INVOLVE SUMS OVER SEVERAL COMPLEX VARIABLES AND ENCODE INTRICATE ARITHMETIC DATA. THESE SERIES GENERALIZE CLASSICAL DIRICHLET SERIES AND ARE STUDIED FOR THEIR CONNECTIONS TO HIGHER RANK GROUPS, REPRESENTATION THEORY, AND ADVANCED ANALYTIC PROPERTIES.

- EXTENSION OF ANALYTIC TECHNIQUES TO MULTIPLE COMPLEX VARIABLES
- CONNECTIONS TO MOMENTS OF L-FUNCTIONS AND RANDOM MATRIX THEORY
- APPLICATIONS IN ARITHMETIC STATISTICS AND ALGEBRAIC GEOMETRY

## FREQUENTLY ASKED QUESTIONS

### WHAT IS A MODULAR FUNCTION IN NUMBER THEORY?

A MODULAR FUNCTION IS A COMPLEX FUNCTION THAT IS INVARIANT UNDER THE ACTION OF A MODULAR GROUP, TYPICALLY DEFINED ON THE UPPER HALF-PLANE, AND EXHIBITS SPECIFIC TRANSFORMATION PROPERTIES UNDER THE GROUP  $SL(2, \mathbb{Z})$ . THEY OFTEN ARISE IN THE CONTEXT OF MODULAR FORMS WITH WEIGHT ZERO.

### HOW ARE MODULAR FUNCTIONS RELATED TO MODULAR FORMS?

MODULAR FUNCTIONS CAN BE SEEN AS MODULAR FORMS OF WEIGHT ZERO. WHILE MODULAR FORMS TRANSFORM IN A SPECIFIC WAY UNDER THE MODULAR GROUP WITH A GIVEN WEIGHT, MODULAR FUNCTIONS ARE INVARIANT UNDER THE GROUP ACTION, ALLOWING POLES ONLY AT THE CUSPS.

### WHAT IS A DIRICHLET SERIES IN NUMBER THEORY?

A DIRICHLET SERIES IS AN INFINITE SERIES OF THE FORM  $\sum_{n=1}^{\infty} a_n / n^s$ , WHERE  $s$  IS A COMPLEX VARIABLE AND  $a_n$  ARE COMPLEX COEFFICIENTS. IT IS A FUNDAMENTAL TOOL IN ANALYTIC NUMBER THEORY FOR STUDYING ARITHMETIC FUNCTIONS AND L-FUNCTIONS.

### HOW DO MODULAR FUNCTIONS CONNECT TO DIRICHLET SERIES?

MODULAR FUNCTIONS AND MODULAR FORMS OFTEN PRODUCE DIRICHLET SERIES THROUGH THEIR FOURIER EXPANSIONS OR ASSOCIATED L-SERIES. THESE DIRICHLET SERIES ENCODE ARITHMETIC INFORMATION AND CAN SATISFY FUNCTIONAL EQUATIONS TIED TO THE MODULARITY PROPERTIES.

### WHAT IS THE SIGNIFICANCE OF THE J-INVARIANT AS A MODULAR FUNCTION?

THE J-INVARIANT IS A FUNDAMENTAL MODULAR FUNCTION THAT CLASSIFIES ELLIPTIC CURVES OVER THE COMPLEX NUMBERS UP TO ISOMORPHISM. IT IS INVARIANT UNDER THE MODULAR GROUP AND PLAYS A CENTRAL ROLE IN THE THEORY OF COMPLEX MULTIPLICATION AND MODULAR FORMS.

## CAN DIRICHLET SERIES ASSOCIATED WITH MODULAR FORMS BE ANALYTICALLY CONTINUED?

YES, DIRICHLET SERIES ARISING FROM MODULAR FORMS, LIKE L-SERIES, OFTEN ADMIT ANALYTIC CONTINUATION TO THE ENTIRE COMPLEX PLANE (EXCEPT POSSIBLY POLES) AND SATISFY FUNCTIONAL EQUATIONS, WHICH ARE CRUCIAL FOR DEEP RESULTS LIKE THE MODULARITY THEOREM.

## WHAT ROLE DO MODULAR FUNCTIONS PLAY IN THE PROOF OF FERMAT'S LAST THEOREM?

MODULAR FUNCTIONS AND MODULAR FORMS WERE KEY IN THE PROOF OF FERMAT'S LAST THEOREM, AS ANDREW WILES PROVED THE MODULARITY OF SEMISTABLE ELLIPTIC CURVES, LINKING THEM TO MODULAR FORMS AND THEIR ASSOCIATED L-SERIES, ESTABLISHING THE TANIYAMA-SHIMURA-WEIL CONJECTURE.

## HOW DO DIRICHLET SERIES HELP IN UNDERSTANDING PRIME NUMBER DISTRIBUTIONS?

DIRICHLET SERIES, PARTICULARLY DIRICHLET L-SERIES, GENERALIZE THE RIEMANN ZETA FUNCTION AND ARE USED TO STUDY PRIMES IN ARITHMETIC PROGRESSIONS. THEIR ANALYTIC PROPERTIES, SUCH AS ZEROS AND POLES, PROVIDE INSIGHTS INTO THE DISTRIBUTION OF PRIME NUMBERS.

## WHAT IS THE MODULARITY THEOREM AND ITS RELATION TO DIRICHLET SERIES?

THE MODULARITY THEOREM STATES THAT EVERY RATIONAL ELLIPTIC CURVE CORRESPONDS TO A MODULAR FORM. THIS CORRESPONDENCE LINKS THE ELLIPTIC CURVE'S L-SERIES, EXPRESSED AS A DIRICHLET SERIES, TO THE MODULAR FORM'S FOURIER COEFFICIENTS, ENABLING DEEP ANALYSIS THROUGH MODULARITY.

## ADDITIONAL RESOURCES

### 1. *MODULAR FUNCTIONS AND DIRICHLET SERIES IN NUMBER THEORY*

THIS CLASSICAL TEXT EXPLORES THE DEEP CONNECTIONS BETWEEN MODULAR FUNCTIONS AND DIRICHLET SERIES, PROVIDING A COMPREHENSIVE INTRODUCTION TO THEIR ROLES IN ANALYTIC NUMBER THEORY. IT COVERS THE THEORY OF MODULAR FORMS, EISENSTEIN SERIES, AND L-FUNCTIONS, WITH DETAILED PROOFS AND EXAMPLES. THE BOOK IS SUITABLE FOR ADVANCED UNDERGRADUATES AND GRADUATE STUDENTS SEEKING A RIGOROUS FOUNDATION.

### 2. *INTRODUCTION TO MODULAR FORMS WITH APPLICATIONS TO DIRICHLET SERIES*

THIS BOOK OFFERS A CLEAR AND ACCESSIBLE INTRODUCTION TO MODULAR FORMS AND THEIR APPLICATIONS TO THE STUDY OF DIRICHLET SERIES. IT EMPHASIZES COMPUTATIONAL TECHNIQUES AND INCLUDES NUMEROUS EXERCISES TO REINFORCE UNDERSTANDING. THE AUTHOR ALSO DISCUSSES THE INTERPLAY BETWEEN MODULARITY AND ANALYTIC PROPERTIES OF L-FUNCTIONS.

### 3. *ANALYTIC NUMBER THEORY: MODULAR FUNCTIONS AND DIRICHLET SERIES*

FOCUSING ON ANALYTIC METHODS IN NUMBER THEORY, THIS VOLUME DELVES INTO THE THEORY OF MODULAR FUNCTIONS AND THEIR ASSOCIATED DIRICHLET SERIES. IT COVERS KEY TOPICS SUCH AS THE MODULAR GROUP, Q-EXPANSIONS, AND THE ANALYTIC CONTINUATION OF L-SERIES. THE TEXT IS WELL-SUITED FOR RESEARCHERS INTERESTED IN THE ANALYTIC ASPECTS OF MODULAR FORMS.

### 4. *MODULAR FORMS AND DIRICHLET SERIES*

THIS COMPREHENSIVE TREATISE PROVIDES AN IN-DEPTH STUDY OF MODULAR FORMS AND THEIR RELATED DIRICHLET SERIES, EXPLORING BOTH CLASSICAL AND MODERN PERSPECTIVES. IT INCLUDES DISCUSSIONS ON HECKE OPERATORS, CUSP FORMS, AND APPLICATIONS TO ARITHMETIC PROBLEMS. THE RIGOROUS APPROACH MAKES IT IDEAL FOR GRADUATE STUDENTS AND PROFESSIONAL MATHEMATICIANS.

### 5. *DIRICHLET SERIES AND MODULAR FORMS IN NUMBER THEORY*

THIS BOOK PRESENTS A DETAILED ACCOUNT OF DIRICHLET SERIES ARISING FROM MODULAR FORMS, HIGHLIGHTING THEIR SIGNIFICANCE IN NUMBER THEORY. IT CAREFULLY DEVELOPS THE THEORY OF MODULAR FUNCTIONS BEFORE CONNECTING IT TO THE

PROPERTIES OF ASSOCIATED L-SERIES. READERS WILL FIND NUMEROUS EXAMPLES ILLUSTRATING THE THEORY'S APPLICATIONS TO PRIME NUMBER DISTRIBUTIONS AND CLASS NUMBERS.

#### 6. *THE THEORY OF MODULAR FUNCTIONS AND DIRICHLET SERIES*

A CLASSIC WORK IN THE FIELD, THIS VOLUME SYSTEMATICALLY DEVELOPS THE THEORY OF MODULAR FUNCTIONS ALONGSIDE THE STUDY OF DIRICHLET SERIES. IT EMPHASIZES THE HISTORICAL DEVELOPMENT AND KEY RESULTS, INCLUDING MODULAR EQUATIONS AND FUNCTIONAL EQUATIONS OF L-FUNCTIONS. THE TEXT IS A VALUABLE RESOURCE FOR THOSE INTERESTED IN THE FOUNDATIONAL ASPECTS OF MODULAR FORMS.

#### 7. *MODULAR FORMS, DIRICHLET CHARACTERS, AND L-SERIES*

THIS TEXT EXPLORES THE RELATIONSHIPS BETWEEN MODULAR FORMS, DIRICHLET CHARACTERS, AND THEIR L-SERIES, PROVIDING INSIGHTS INTO CHARACTER SUMS AND MODULAR TRANSFORMATIONS. IT INCLUDES COMPREHENSIVE PROOFS AND APPLICATIONS TO PROBLEMS IN ANALYTIC NUMBER THEORY. THE BOOK IS TAILORED FOR GRADUATE-LEVEL COURSES AND RESEARCH.

#### 8. *ADVANCED TOPICS IN MODULAR FUNCTIONS AND DIRICHLET SERIES*

DESIGNED FOR ADVANCED READERS, THIS BOOK COVERS SPECIALIZED TOPICS SUCH AS THE RANKIN-SELBERG METHOD, PETERSSON INNER PRODUCTS, AND NON-HOLOMORPHIC MODULAR FORMS. IT INVESTIGATES THE ANALYTIC PROPERTIES OF DIRICHLET SERIES CONNECTED TO THESE MODULAR OBJECTS. THE VOLUME IS IDEAL FOR RESEARCHERS SEEKING TO DEEPEN THEIR UNDERSTANDING OF MODERN DEVELOPMENTS.

#### 9. *MODULAR FORMS AND THEIR DIRICHLET SERIES: A COMPUTATIONAL APPROACH*

FOCUSING ON COMPUTATIONAL METHODS, THIS BOOK PROVIDES TOOLS AND ALGORITHMS FOR STUDYING MODULAR FORMS AND THEIR ASSOCIATED DIRICHLET SERIES. IT BRIDGES THEORETICAL CONCEPTS WITH PRACTICAL COMPUTATION, INCLUDING SOFTWARE IMPLEMENTATIONS AND NUMERIC EXAMPLES. THIS TEXT IS PARTICULARLY USEFUL FOR MATHEMATICIANS INTERESTED IN EXPERIMENTAL AND COMPUTATIONAL NUMBER THEORY.

## **Modular Functions And Dirichlet Series In Number Theory**

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